

Exponentials- Study Guide

1. Label and explain the following exponential equations:

a) $y = ab^x$

Labels: a → Initial Value, b → Change factor, x → Time, y → Total

b) $y = a(1 \pm r)^x$

Labels: a → Initial Value, $(1 \pm r)$ → Change factor, x → time, r → % rate, y → Total

c) $y = ab^{x-h} + k$

Labels: a → Stretch / Compress / flip
 > 1 stretch, fraction compress, - flip
 b → Growth / Decay
 > 1 Growth, fraction Decay
 h → horizontal left / right
 - left, + right
 k → Vertical up / down
 + up, - down

Determine whether the table represents an exponential growth function, an exponential decay function, linear, or neither. Make sure to explain your reasoning.

2.

x	0	1	2	3
y	2	4	12	48

Annotations: $+1, +1, +1$ (x); $\times 2, \times 3, \times 4$ (y); $+2, +8, +36$ (y)

Neither The y's are not multiplying by a constant factor. Also not adding by a constant value

3.

x	0	1	2	3
y	270	90	30	10

Annotations: $+1, +1, +1$ (x); $\div 3, \div 3, \div 3$ (y)

Exponential Decay
 The y values are being divided by a constant factor

4.

x	-1	0	-1	-2
y	-4	0	4	8

Annotations: $+1, -1, -1$ (x); $+4, +4, +4$ (y)

Neither
 The x values are not changing by a constant value

Find the value of $a, b,$ and $r.$ Determine whether the data represents an exponential growth function, an exponential decay function. Make sure to explain your reasoning.

5. $y = 3(.85)^x$

$a = 3$
 $b = .85$
 $r = .15$

Exponential decay because the change factor is less than 1

6. $y = 3(1 - .3)^x$

$a = 3$
 $b = .7$
 $r = .3$

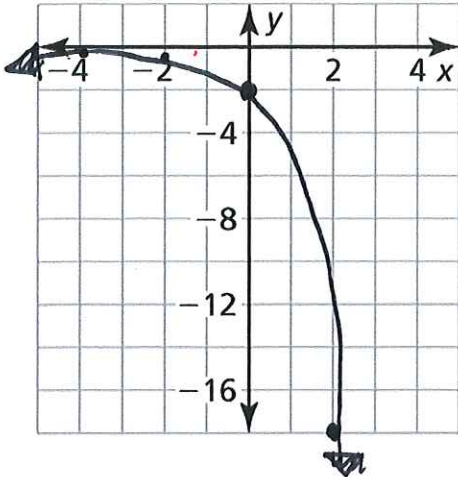
Exponential Decay because the rate is being subtracted.

7. $y = 2(1.4)^x$

$a = 2$
 $b = 1.4$
 $r = .4$

Exponential Growth because the change factor is greater than 1

8. Graph $y = -2(3)^x$



x	y
-4	-0.024
-2	-0.22
0	-2
2	-18
4	-162

$$y = -2(3)^{-4}$$

$$y = -2(.0123)$$

$$y = -.024$$

$$y = -2(3)^{-2}$$

$$y = -2(.11)$$

$$y = -.222$$

$$y = -2(3)^0$$

$$y = -2(1)$$

$$y = -2$$

$$y = -2(3)^2$$

$$y = -2(9)$$

$$y = -18$$

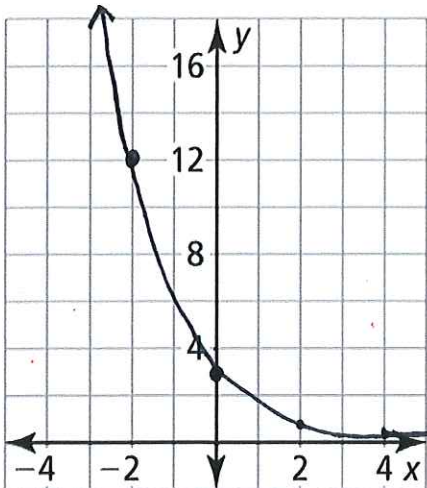
$$y = -2(3)^x$$

$$y = -2(3)^4$$

$$y = -2(81)$$

$$y = -162$$

9. Graph $y = 3(0.5)^x$



x	y
-4	48
-2	12
0	3
2	.75
4	.1875

$$y = 3(.5)^{-4}$$

$$y = 3(16)$$

$$y = 48$$

$$y = 3(.5)^{-2}$$

$$y = 3(4)$$

$$y = 12$$

$$y = 3(.5)^0$$

$$y = 3(1)$$

$$y = 3$$

$$y = 3(.5)^2$$

$$y = 3(.25)$$

$$y = .75$$

$$y = 3(.5)^4$$

$$y = 3(.0625)$$

$$y = .1875$$

Evaluate the function for the given value of x .

10. $y = 2^x; x = 5$

$$y = 2^5$$

$$y = 32$$

11. $f(x) = 3(4)^x; x = -1$

$$f(-1) = 3(4)^{-1}$$

$$f(-1) = 3\left(\frac{1}{4}\right)$$

$$f(-1) = \frac{3}{4}$$

$$f(-1) = .75$$

12. $y = -4(2)^x; x = -3$

$$y = -4(2)^{-3}$$

$$y = -4\frac{1}{2^3}$$

$$y = -4\left(\frac{1}{8}\right)$$

$$y = -\frac{4}{8}$$

$$y = -\frac{1}{2}$$

$$y = -.5$$

13. $f(x) = 5(3)^x; x = 0$

$$f(0) = 5(3)^0$$

$$f(0) = 5(1)$$

$$f(0) = 5$$

Write an equation to model the situation. Be sure to label the parts of your equation.

1. You are brushing your teeth and you have 4 bacterial. They double every hour.

$$y = 4(2)^x$$

Labels: y → Total Bacteria; 4 → Initial Bacteria in Mouth; 2 → change factor; x → hours

2. You have 5 weeds in the yard. They triple every hour.

$$y = 5(3)^x$$

Labels: y → Total # of Weeds; 5 → Initial # of Weeds; 3 → change factor; x → hour

3. There are 3 zombies. They increase by 10% every hour.

$$y = 3(1 + .10)^x$$

Labels: y → Total Zombies; 3 → initial # of Zombies; $1 + .10$ → % change; x → hour

4. There were once 1,000 dodo birds. Their population was cut down by 15% every day.

$$y = 1,000(1 - .15)^x$$

Labels: y → Total # of Birds; $1,000$ → Initial # of dodo birds; $1 - .15$ → % rate; x → day